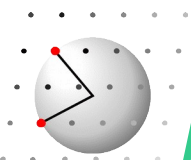




tutorial session IV

short range order
SRO





Short range order SRO



in disordered crystals “objects” are often ordered only at a short range distance

neighbours are not strictly periodic but present only with a given probability

example in 1-D chain



A A A B A B A B A A A B B A A B B B B A B

assumptions: objects are simple atoms
interatomic distances are strictly periodic

possible pairs are

AA	with	P_n^{AA}	P_n^{ij} probability to find a pair ij $n = 1, 2, \dots$ distance in $n \cdot a$
AB	with	P_n^{AB}	
BA	with	P_n^{BA}	
BB	with	P_n^{BB}	

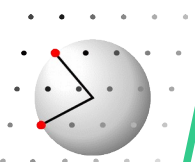
relative occupations: m_A and m_B $0 \leq m_A \leq 1$
 $m_A + m_B = 1$

influence of probabilities on diffraction pattern ?

what does a structure look like for different probabilities ?

is any value for the probabilities allowed ?

connection between probabilities and occupation with A / B ?



Short range order SRO



A A A B A B A B A A A B B A A B B B A B

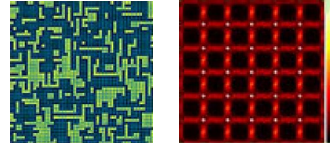
Pair- pair correlation terms describe the probability P_n^{AA}
independent of chemical composition

$C_n = (P_n^{AA} - m_A^2) / (m_A m_B)$ pair correlation coefficient for atoms at distance n

$C_n = 0$ If distributed at random: $P_n^{AA} = m_A^2$

$C_n > 0$ $P_n^{AA} > m_A^2$ preferably equal neighbors **AA** and **BB**

$C_n < 0$ $P_n^{AA} < m_A^2$ preferably different neighbors **AB** and **BA**



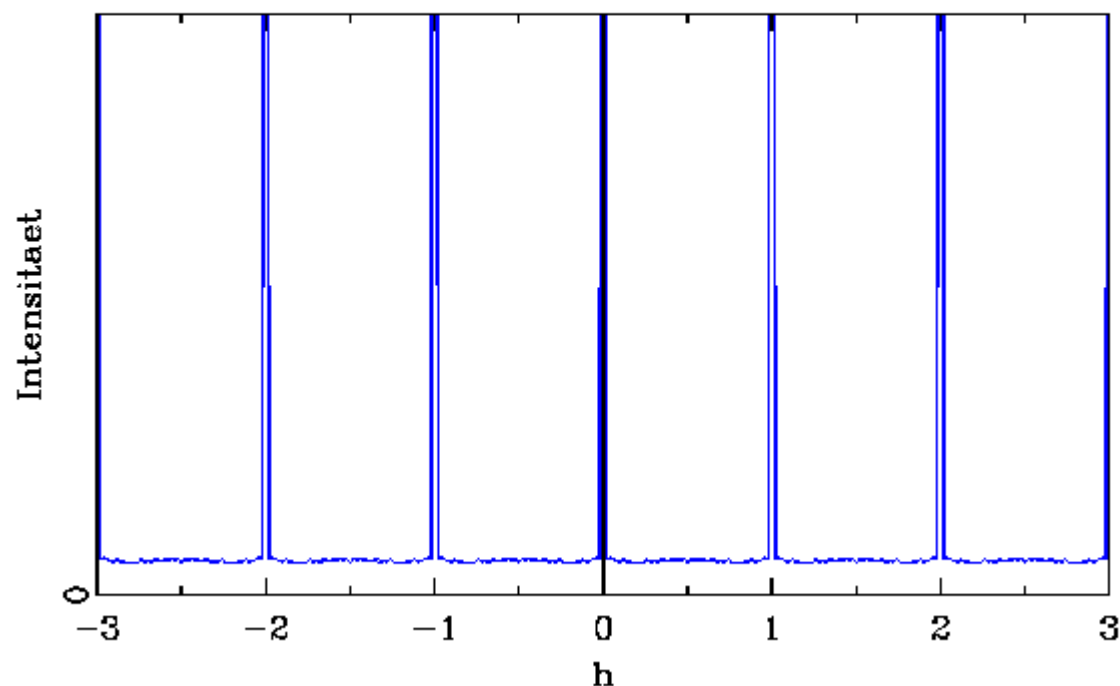
Short range order SRO



$C_n = 0$ $m_A = 0.5$ random sequence

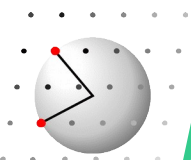


completely random
sequence of the atoms



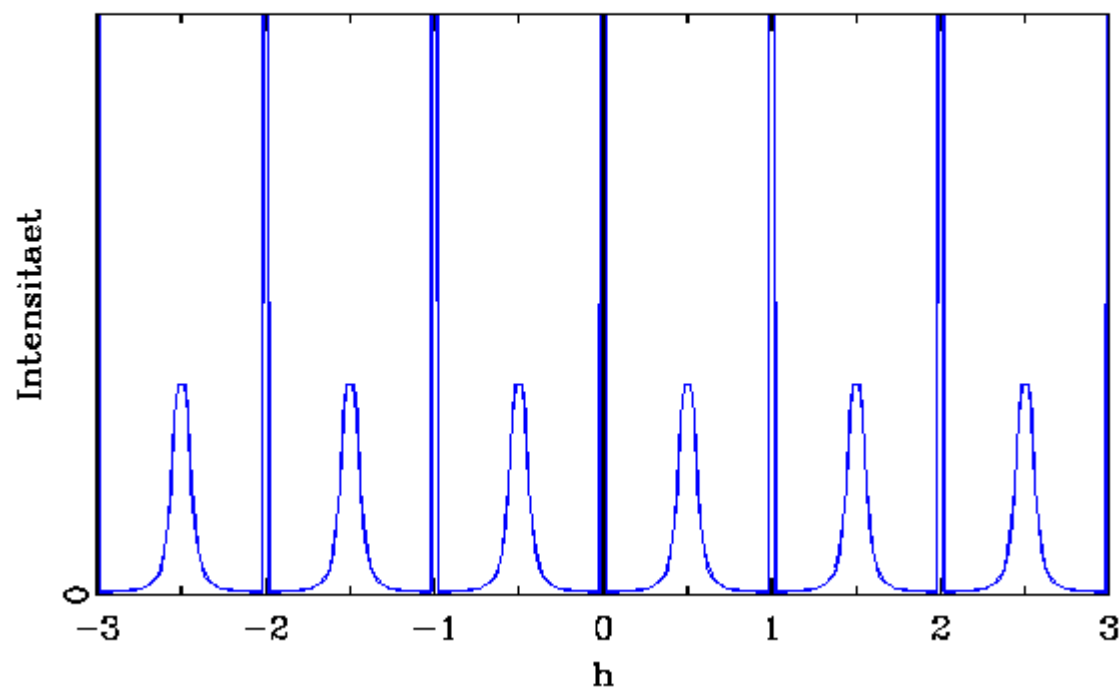
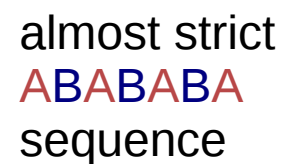
sharp Bragg peaks
at integer h

simple continuous
diffuse background





$$C_n = -1 \quad m_A = 0.5$$

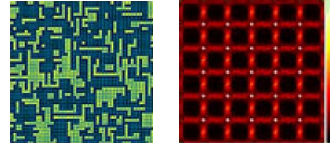


sharp Bragg peaks
at integer h

diffuse scattering
maxima at $h=1/2$

Clear trend to form a period of 2a





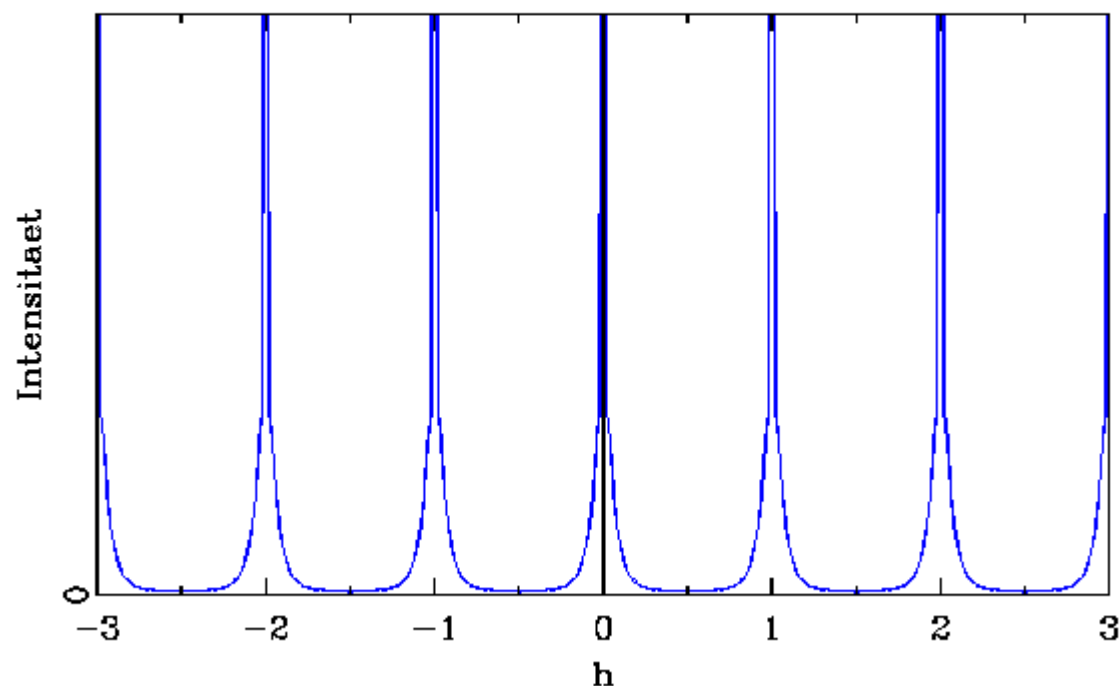
Short range order SRO



$$C_n = 1 \quad m_A = 0.5$$



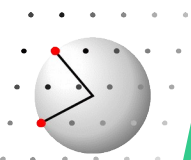
almost strict
AAABBBBA
sequence

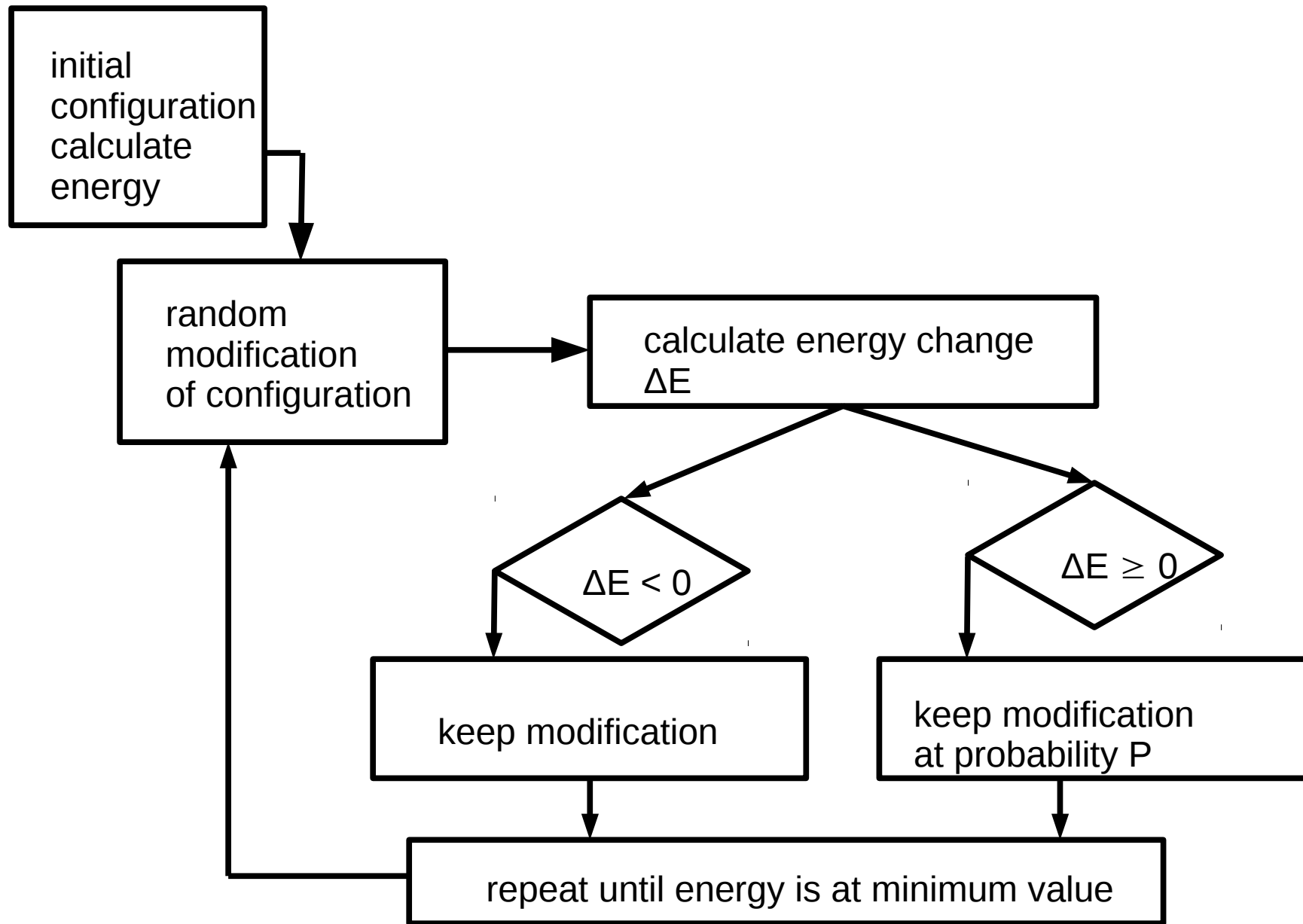


sharp Bragg peaks
at integer h

diffuse scattering
maxima at integer h

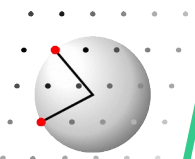
clear tendency to form domains with periodicity **a**





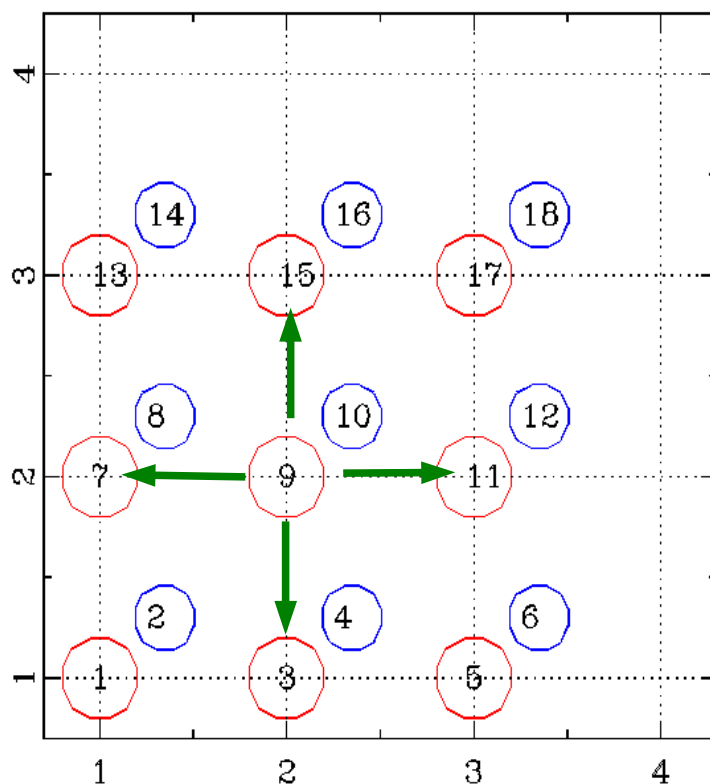


neighbourhood	which atoms are correlated distance, list of interatomic vectors, ...
correlations	how are atoms related to each other ? chemical equal atoms \Leftrightarrow different distance distance between atom pairs angular bond angle in triplet
modification	how is the crystal structure changed switch two atoms shift individual atoms
Monte Carlo	details of the process number of refinement cycles pseudotemperature kT





Y - axis



X - axis

Neighbors for atom 9

3: site **1** in $[0, -1, 0]$

7: site **1** in $[-1, 0, 0]$

11: site **1** in $[1, 0, 0]$

15: site **1** in $[0, 1, 0]$

in „chem“ and „mmc“ menus

set vect, 1, **1**, **1**, **0**, **-1**, **0**

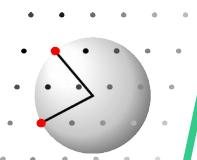
set vect, 2, **1**, **1**, **-1**, **0**, **0**

set vect, 3, **1**, **1**, **1**, **0**, **0**

set vect, 4, **1**, **1**, **0**, **1**, **0**

This will describe ALL neighbors
of site **1** in any unit cell!

Very fast algorithm to address atoms!





```
# create a structure with randomly distributed atoms...
#
mmc
  set neig,rese                      reset neighborhood
#
  set vec,1, 1,1, 1, 0, 0           Atoms are separated by vector[1,0,0]
                                     Pairs are 1st atoms in any unit cell
  set vec,2, 1,1, -1, 0, 0
  set neig,vec,1,2                 Vector definitions 1,2 are one neighborhood
#
  set mode, 1.0, swchem,all        Switch any atom pairs with probability 1.0
#
  set targ,1,corr,cu,void, 0.90 ,0.0,CORR    Correlation energy no. is
                                               chemical between Cu and voids
                                               Target is a C = 0.90
#
  set cyc, 100*n[1]                  No. of cycles is 100 time no. of atoms
  set feed, 5*n[1]
  set temp, 2.0                      Temperature kT = 2.0
  run                                start the calculation
exit
#
```



Binary System with two atom types

Composition 50:50

First neighbor correlations only:

$[1, 0, 0]; [\bar{1}, 0, 0]$

$[0, 1, 0]; [0, \bar{1}, 0]$

$[1, 1, 0]; [\bar{1}, 1, 0]$

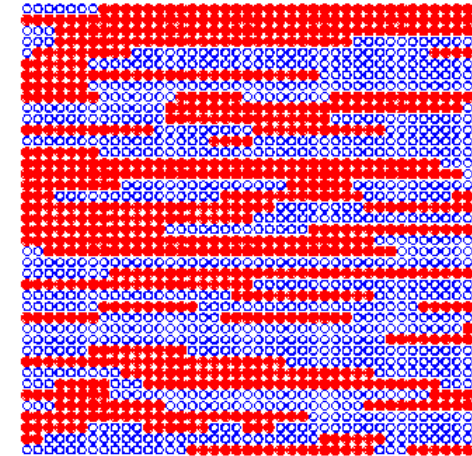
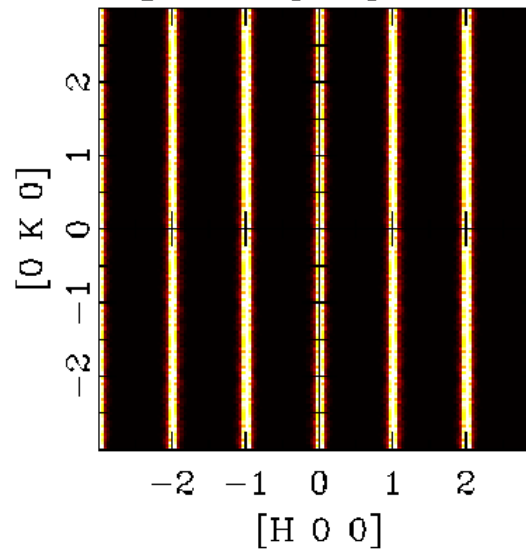
$[1, 1, 0]; [1, 1, 0]$

Chemical short range order

Target:

$$C[1, 0, 0] = 1.0$$

Ziel $C[100] = 1.00$
Ergebnis $C[100] = 0.90$



$C[100] = 0.90$
 $C[010] = 0.02$
 $C[110] = 0.02$
 $C[-110] = 0.00$

Binary System with two atom types

First neighbor correlations only:

$$[1, 0, 0]; [\bar{1}, 0, 0]$$

$$[0, 1, 0]; [0, \bar{1}, 0]$$

$$[1, \bar{1}, 0]; [\bar{1}, 1, 0]$$

$$[1, 1, 0]; [\bar{1}, \bar{1}, 0]$$

Composition 50:50

Chemical short range order

Target:

$$C[1, 0, 0] = 1.0$$

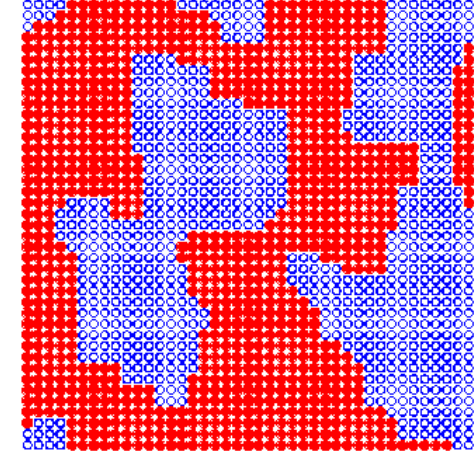
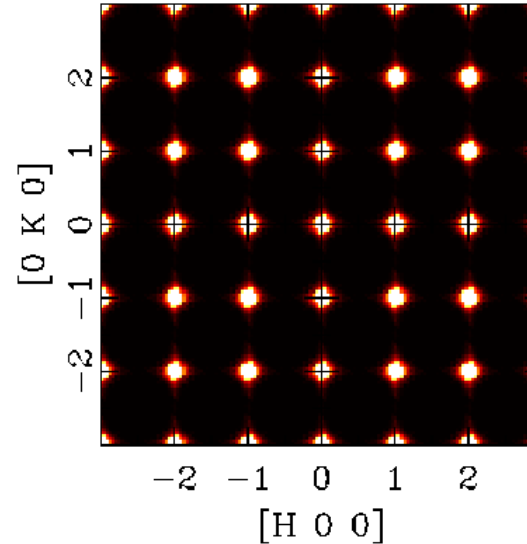
$$C[0, 1, 0] = 1.0$$

Consequence:

$$C[1, \bar{1}, 0] = 1.0$$

$$C[\bar{1}, 1, 0] = 1.0$$

Ziel $C[100] = 1.00$ $C[010] = 1.00$
 Ergebnis $C[100] = 0.85$ $C[010] = 0.85$



$C[100] = 0.85$
 $C[010] = 0.85$
 $C[110] = 0.76$
 $C[\bar{1}\bar{1}0] = 0.77$

Binary System with two atom types

First neighbor correlations only:

$$[1, 0, 0]; [\bar{1}, 0, 0]$$

$$[0, 1, 0]; [0, \bar{1}, 0]$$

$$[1, \bar{1}, 0]; [\bar{1}, 1, 0]$$

$$[1, 1, 0]; [\bar{1}, \bar{1}, 0]$$

Target:

$$C[1, 0, 0] = 1.0$$

$$C[0, 1, 0] = 1.0$$

$$C[1, \bar{1}, 0] = -1.0$$

$$C[1, 1, 0] = -1.0$$

Consequence:

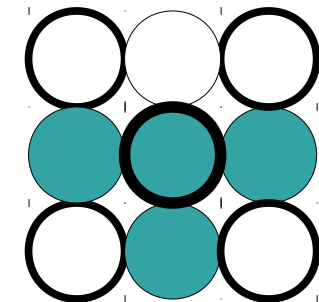
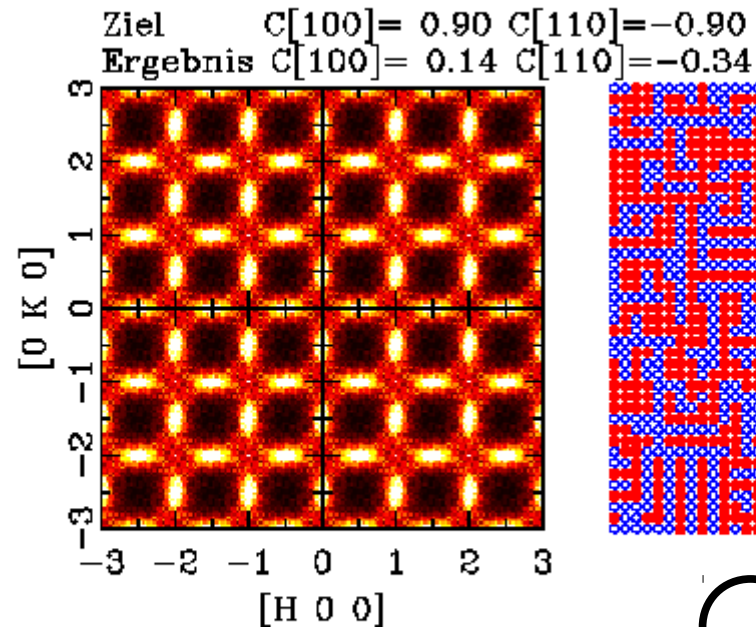
$$C[1, \bar{1}, 0] = 0.14$$

$$C[1, 1, 0] = -0.34$$

Contradictory requests!

Composition 50:50

Chemical short range order



Binary System with two atom types

Composition 50:50

First AND second neighbor

Chemical short range order

$[1, 0, 0]; [\bar{1}, 0, 0]$

$[2, 0, 0]; [2, 0, 0]$

Target:

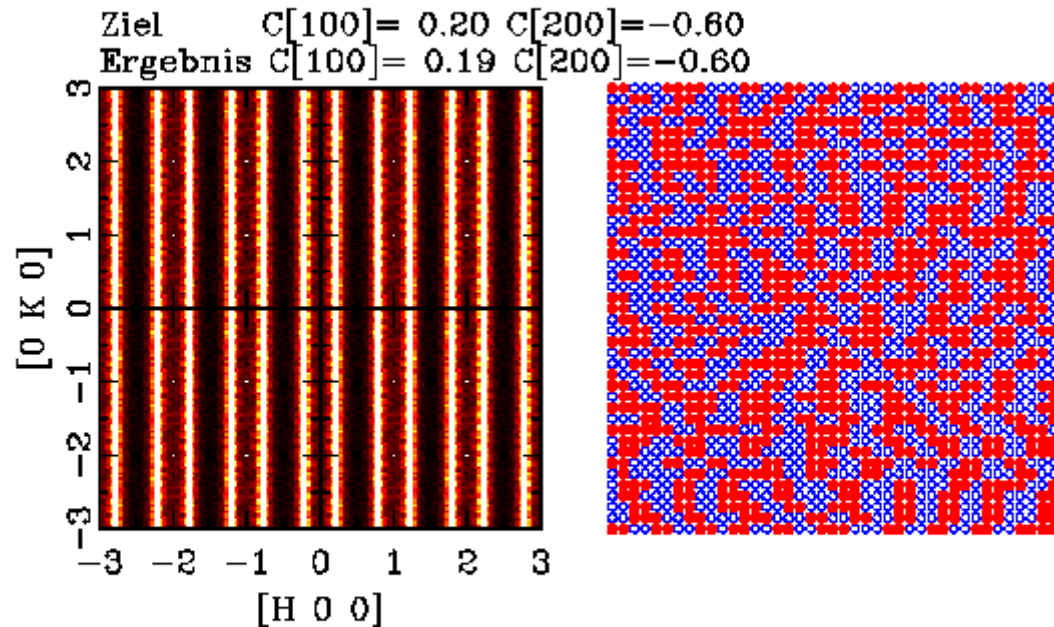
$C[1, 0, 0] = 0.2$

$C[2, 0, 0] = -0.6$

Consequence:

Tendency to form pairs

AA BB AA ...

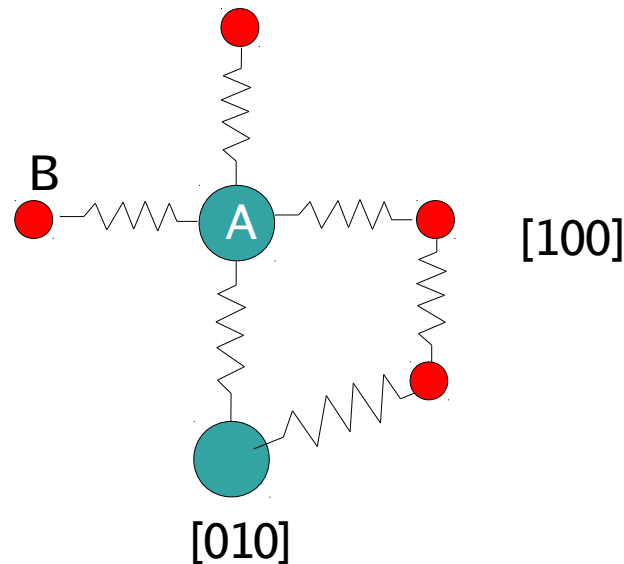
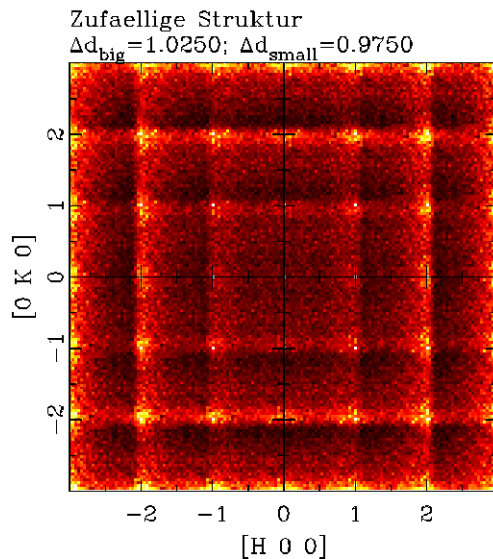


Distance Correlations:

Potential between atom pairs:
$$U(r) = \frac{A}{r^{12}} - \frac{B}{r^6}$$

Angular potential:
$$U(\Theta) = K(\Theta - \Theta_0)^2$$

Radii: $r_A > r_B$



Form factors $f_A > f_B$

Asymmetrically shaped diffuse scattering
 Higher intensity at smaller values of h
 “size effect”



Run discus_suite

Change to directory:

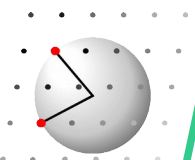
Lectures/04.SRO/SRO_1

Use macro: sro.1 with two parameters: <correlation>, <Temperature>

suite> @sro.1.mac 0.8, 5.1

suite> @sro.1.mac -0.7, 5.1

**Be creative with the
Parameters!**



Run discus_suite

Change to directory:

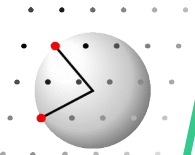
Lectures/04.SRO/SRO_4

Use macro: sro.4.mac with two parameters: <strain>, <Temperature>

suite> @sro.4.mac 0.05, 5.1

suite> @sro.4.mac -0.05, 5.1

**Be creative with the
Parameters!**



Run discus_suite

Change to directory:

Lectures/04.SRO/SRO_3

Use macro: sro.1 with six parameters:

<composition>, <c100>, <c010>, <c110>, <c $\bar{1}$ 10>, <Temperature>

```
suite> @sro.3.mac 0.5, 0.4, 0.4, 0.3, 0.3, 1.0
```

```
suite> @sro.3.mac 0.5,-0.7, 0.8, -0.6, 0.9, 1.0
```

**Be creative with the
Parameters!**

